We are assuming that:

To integrate out, we have that:

Notice that this is the result of integrating out for a single group. Therefore, we need on of this for every group.